

D&A of changes in extremes

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Photo: F. Zwiers

Introduction

- Yesterday's talk
 - Detection and attribution of change in the mean state
 - Science using this technique has become the foundation for the series of attribution assessments that have been made by the IPCC
 - SAR – 1995 – “discernable evidence”
 - AR5 – 2013 – it is “extremely likely that most ...”
- Today's talk
 - Detection and attribution of changes in extremes
 - Event attribution
- Key reference
 - [WCRP summer school on extremes](#), ICTP, July, 2014

Outline

- Brief review
- Example of trend detection
- Event attribution
- Discussion

Photo: F. Zwiers (Marsh Wren)

Definition of D & A

- *Detection* of change is defined as the process of demonstrating that climate or a system affected by climate has changed in some defined statistical sense without providing a reason for that change.
- *Attribution* is defined as the process of evaluating the relative contributions of multiple causal factors to a change or event with an assignment of statistical confidence.
- In WG1, casual factors usually refer to *external influences*, which may be *anthropogenic* (GHGs, aerosols, ozone precursors, land use) and/or *natural* (volcanic eruptions, solar cycle modulations).

Methods

- Involve simple statistical models
- Complex implementation due to data volumes (which are both small and large)

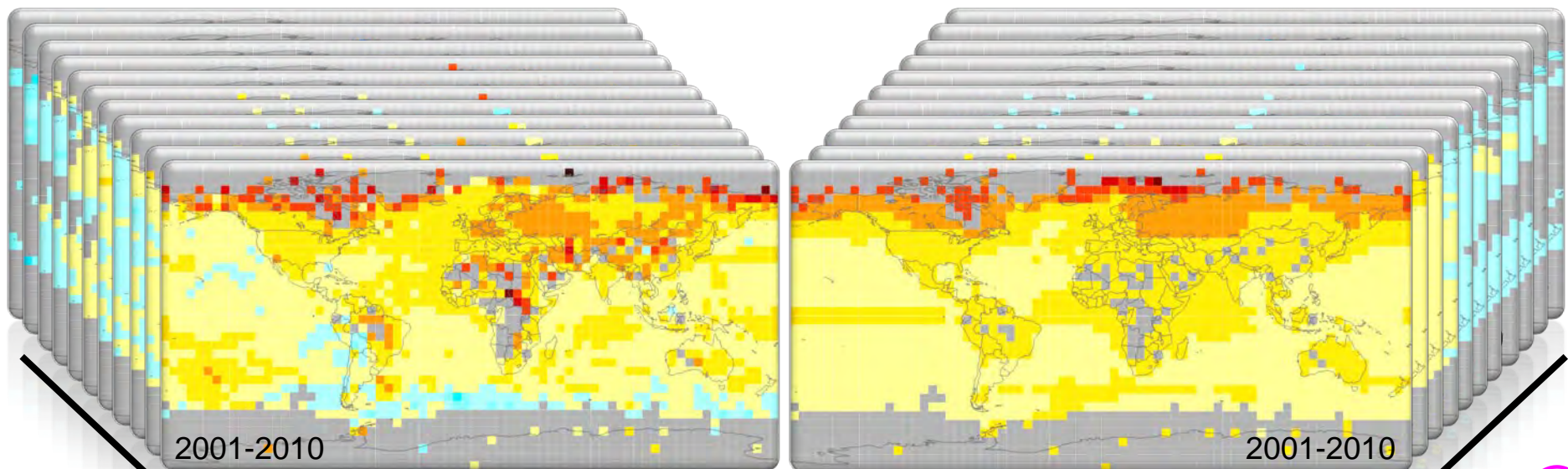
Usual assumptions

- Key forcings have been identified
- Signals and noise are additive
- The large-scale patterns of response are correctly simulated by climate models, but signal amplitude is uncertain

→ leads to a regression formulation

Observations (HadCRUT4)

Multi-model mean (ALL forcings)



11 decades (1901-1911 to 2001-2011)

Y

X

$$Y = X\beta + \varepsilon$$

Evaluate
scaling factors

$\hat{\beta}$

Evaluate
residuals

$\hat{\varepsilon}$

After Weaver and Zwiers (2000)

A temperature extremes example



An approach to D&A on extremes using EV theory

- Several available indices are “block maxima”
 - Temperature: TN_n , TX_n , TN_x , TX_x
 - Precipitation: RX_{1day} , RX_{5day}
- Suggests using the “Generalized Extreme Value” (GEV) distribution, and incorporating the effects of forcing via its parameters
- An example is Zwiers et al, [2011](#)

GEV distribution

- Based on limit theory which predicts that the distribution of block maxima will converge to a *Generalized Extreme Value* distribution as blocks become large
- Distribution function

$$F(y|\mu, \sigma, \xi) = \begin{cases} \exp\left[-\exp\left\{-\frac{y-\mu}{\sigma}\right\}\right], & \xi = 0 \\ \exp\left[-\left\{1 + \xi\frac{y-\mu}{\sigma}\right\}^{-1/\xi}\right], & \xi \neq 0, 1 + \xi\frac{y-\mu}{\sigma} > 0 \end{cases}$$

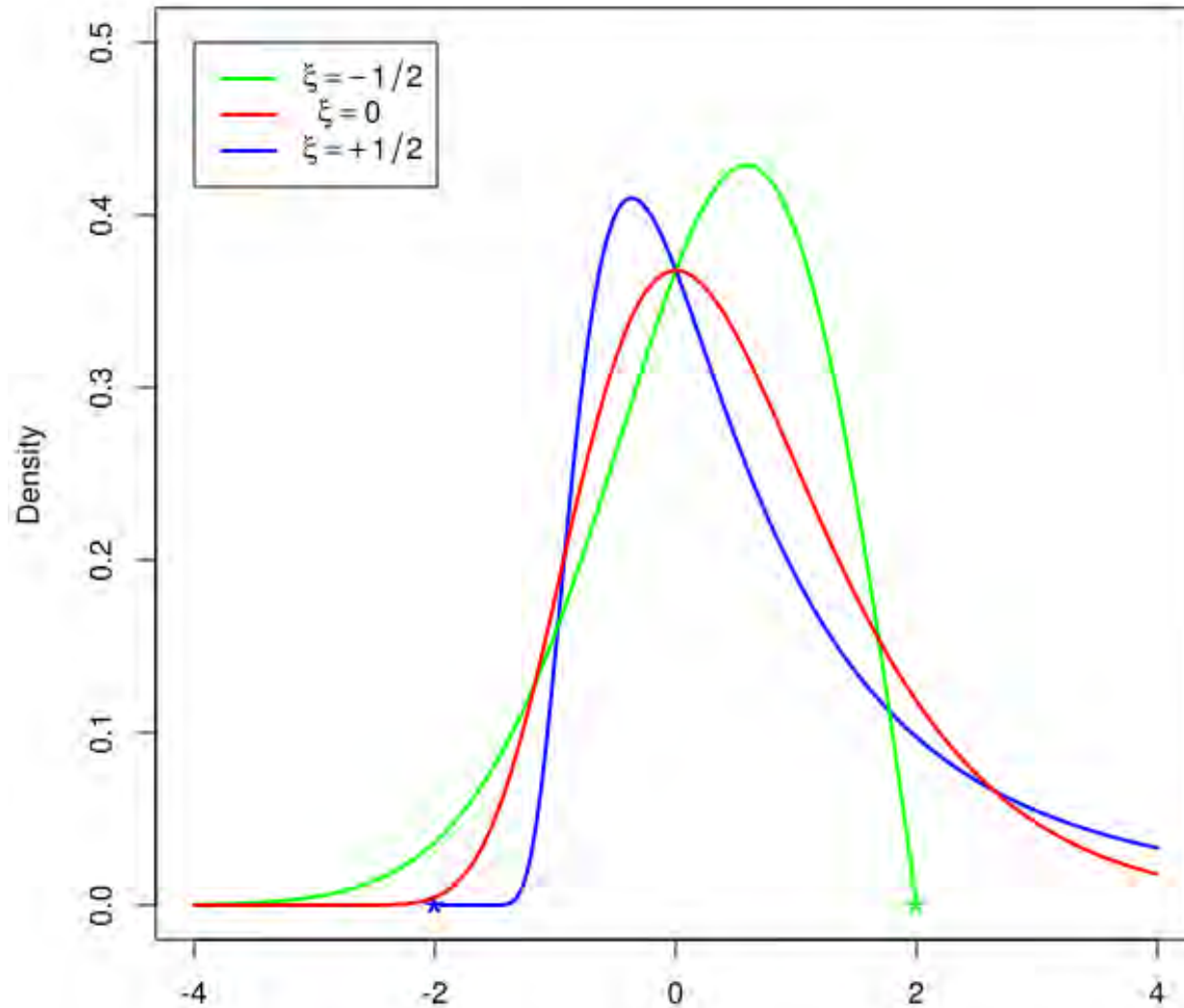
- m -block return value (blocks are often years)

$$y_m = \begin{cases} \mu - (\sigma/\xi) \left\{1 - \left[-\ln\left(1 - \frac{1}{m}\right)\right]^{-\xi}\right\} & \xi \neq 0 \\ \mu - \sigma \ln\left[-\ln\left(1 - \frac{1}{m}\right)\right] & \xi = 0 \end{cases}$$

- Density function

$$f(y|\mu, \sigma, \xi) = \begin{cases} \frac{1}{\sigma} \exp\left[-\frac{y-\mu}{\sigma} - \exp\left(-\frac{y-\mu}{\sigma}\right)\right], & \xi = 0 \\ \frac{1}{\sigma} \left(1 + \xi\frac{y-\mu}{\sigma}\right)^{-1-1/\xi} \exp\left[-\left(1 + \xi\frac{y-\mu}{\sigma}\right)^{-1/\xi}\right], & \xi \neq 0, 1 + \xi\frac{y-\mu}{\sigma} > 0 \end{cases}$$

Generalized extreme value densities



All with $\mu = 0$, $\sigma = 1$. Asterisks mark support-endpoints

Weibull $\xi < 0$
Gumbel $\xi = 0$
Fréchet $\xi > 0$

Working assumption for D&A

- External forcing affects only the GEV location parameter μ
- Parallel to the regression approach
 - Estimates the conditional mean (“location parameter”) of the Gaussian distribution

How do we get the expected pattern of change in μ ?

- For a given climate model and forcing, assume M runs
- 10M years of output for each decade
 - 10M block maxima x_{tlk} for decade t at grid box k
- $t=1, \dots, N$ decades
 - $l=1, \dots, 10M$ simulated years for decade t
- Use these 10M block maxima to estimate GEV parameters for decade t at grid box k
 - estimate N+2 parameters μ_{tk} , σ_k and ξ_k at each grid box
- Do this via maximum likelihood

Estimation of μ_{tk} , σ_k and ξ_k

Maximize the joint likelihood

$$\begin{aligned} L(\mu_{1k}, \dots, \mu_{Nk}, \sigma_k, \xi_k | x_{tlk}, t = 1, \dots, N, l = 1, \dots, 10M) \\ &= \prod_{t=1}^N \prod_{l=1}^{10M} f(x_{tlk} | \mu_{tk}, \sigma_k, \xi_k) \\ &= \prod_{t=1}^N \prod_{l=1}^{10M} \frac{1}{\sigma_k} \left[1 + \xi_k \left(\frac{x_{tlk} - \mu_{tk}}{\sigma_k} \right) \right]^{-1-1/\xi_k} \exp \left\{ - \left[1 + \xi_k \left(\frac{x_{tlk} - \mu_{tk}}{\sigma_k} \right) \right]^{-\frac{1}{\xi_k}} \right\} \end{aligned}$$

Equivalently, minimize the negative log-likelihood

$$-\ln(L) = \sum_{\substack{t=1, \dots, N \\ l=1, \dots, 10M}} \left\{ \ln(\sigma_k) + \left(1 + \frac{1}{\xi_k} \right) \ln \left[1 + \xi_k \left(\frac{x_{tlk} - \mu_{tk}}{\sigma_k} \right) \right] + \left[1 + \xi_k \left(\frac{x_{tlk} - \mu_{tk}}{\sigma_k} \right) \right]^{-\frac{1}{\xi_k}} \right\}$$

Do this at individual grid boxes k

How do we model the observed extremes?

- Use the GEV distribution
 - we have observed block maxima $y_{tk}, t = 1961, \dots, 2000$
- Make the location parameter signal-dependent as follows

$$\mu_{tk}^o = \mu_{t_0k}^o + \beta (\tilde{\mu}_{tk}^m - \tilde{\mu}_{t_0k}^m)$$

$$\text{where } \begin{cases} t = t_0, \dots, 2000, t_0 = 1961 \\ \mu' \text{'s constant within decades} \end{cases}$$

and $\tilde{\mu}_{tk}^m$ is the multi-model ensemble mean of the location parameter estimates for grid box k in decade t from the forced simulations

- Parameters to be estimated from obs are $\mu_{t_0k}^o, \sigma_k^o, \xi_k^o, \beta$
- Note that β is the same at all locations k

Fit the GEV distribution to observations at all grid boxes simultaneously by minimizing

$$-\ln(L) = -\sum_k \ln(L_k)$$

where

$$\begin{aligned} -\ln(L_k) &= (T - t_0 + 1)\ln(\sigma_k^o) \\ &+ \left(1 + \frac{1}{\xi_k^o}\right) \sum_{t=t_0}^T \ln \left[1 + \xi_k^o \left(\frac{y_{tk} - \mu_{t_0k}^o - \beta \Delta \tilde{\mu}_{tk}^m}{\sigma_k^o} \right) \right] \\ &+ \sum_{t=t_0}^T \left[1 + \xi_k^o \left(\frac{y_{tk} - \mu_{t_0k}^o - \beta \Delta \tilde{\mu}_{tk}^m}{\sigma_k^o} \right) \right]^{-1/\xi_k^o} \end{aligned}$$

Do this using the profile likelihood technique

Parallels with standard D&A

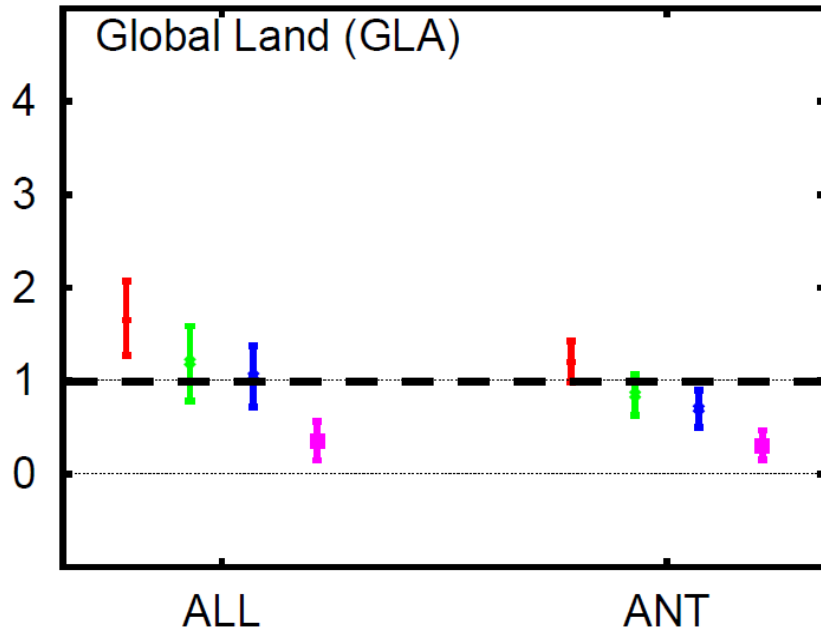
- Single scaling factor to modify the space-time pattern of change in model simulated location parameters
- Like OLS rather than TLS because we don't take uncertainty in model derived location factors into account
- Non-optimized because the likelihood function does not represent dependence between extremes at different locations

Unlike standard D&A

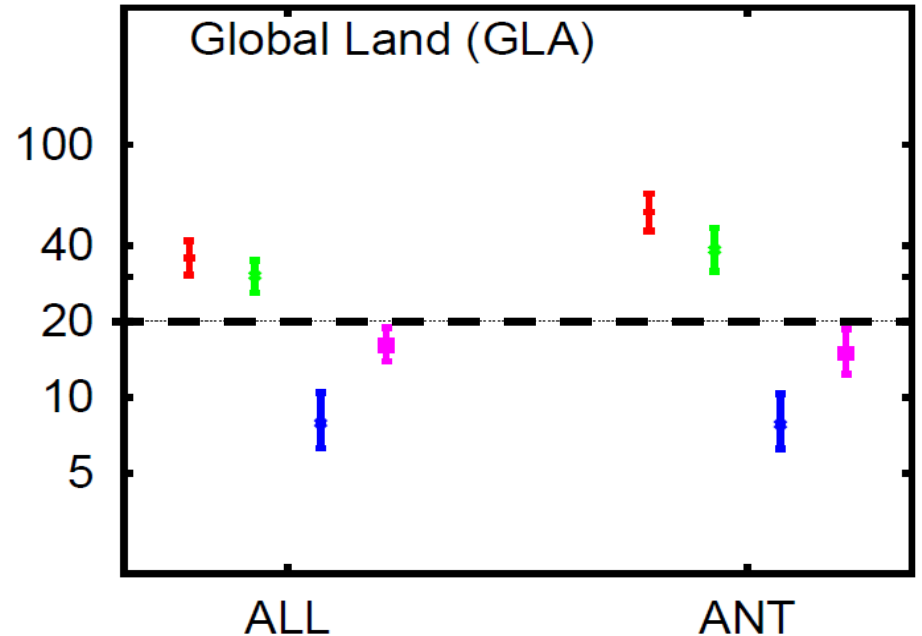
- Uncertainty analysis was not based on control variability because daily output was not available from CMIP3 control runs – used a block bootstrap approach instead

Global Results

Scaling factors and bootstrapped 5-95% uncertainty ranges

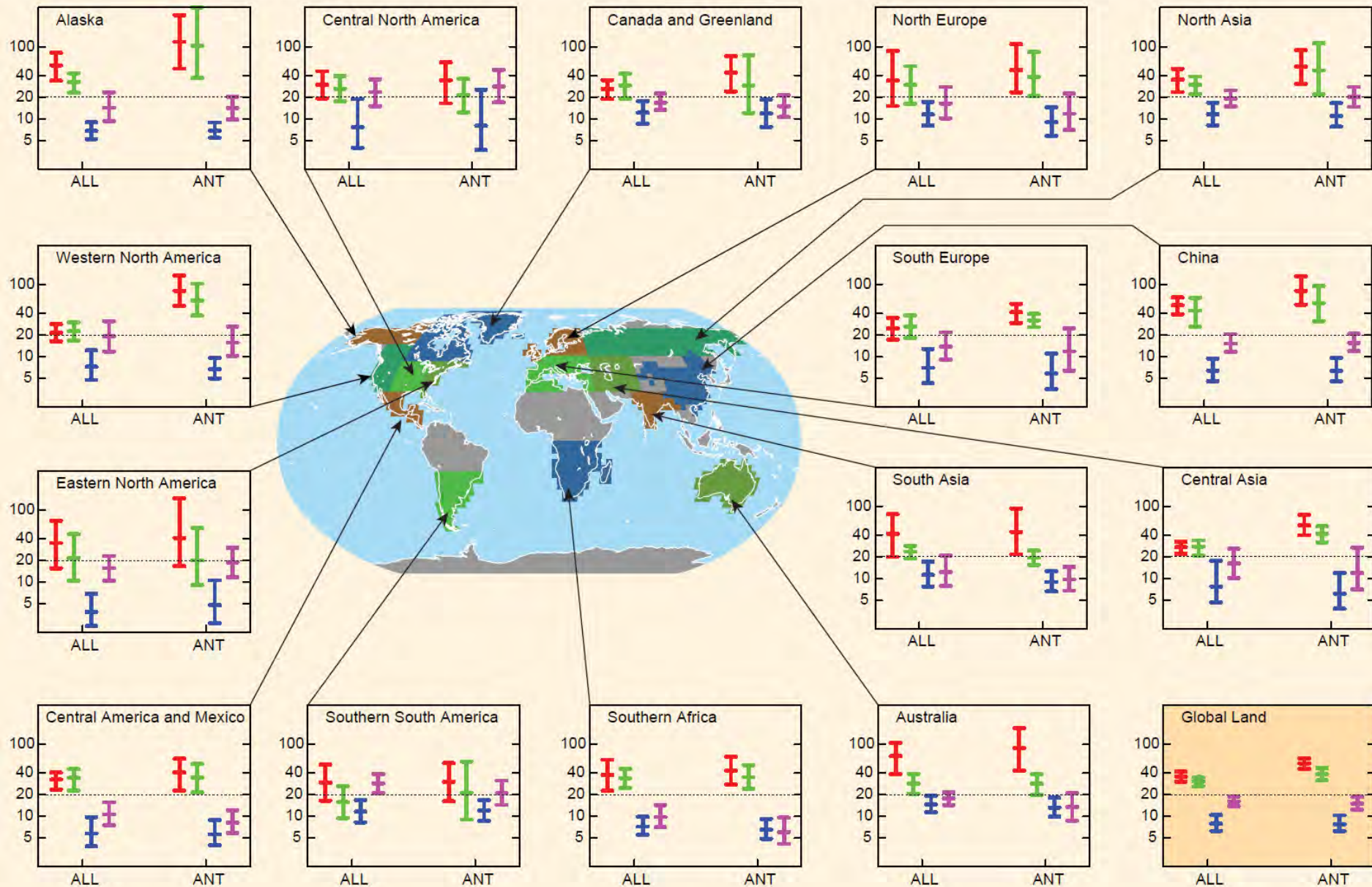


Implied change in waiting times for 20-year event (1990's vs 1960's)



TNn, TXn, TNx, TXx

Implied changes in waiting times (1990's vs 1960's)



Event attribution

The public asks:

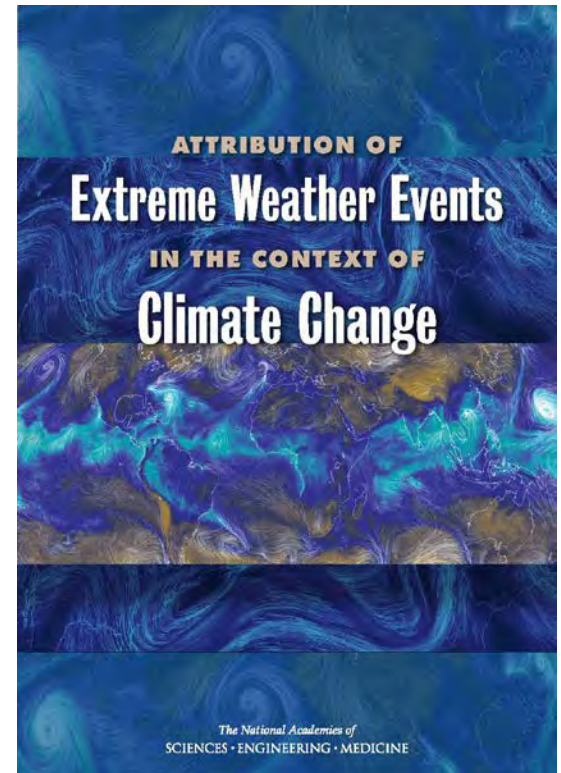
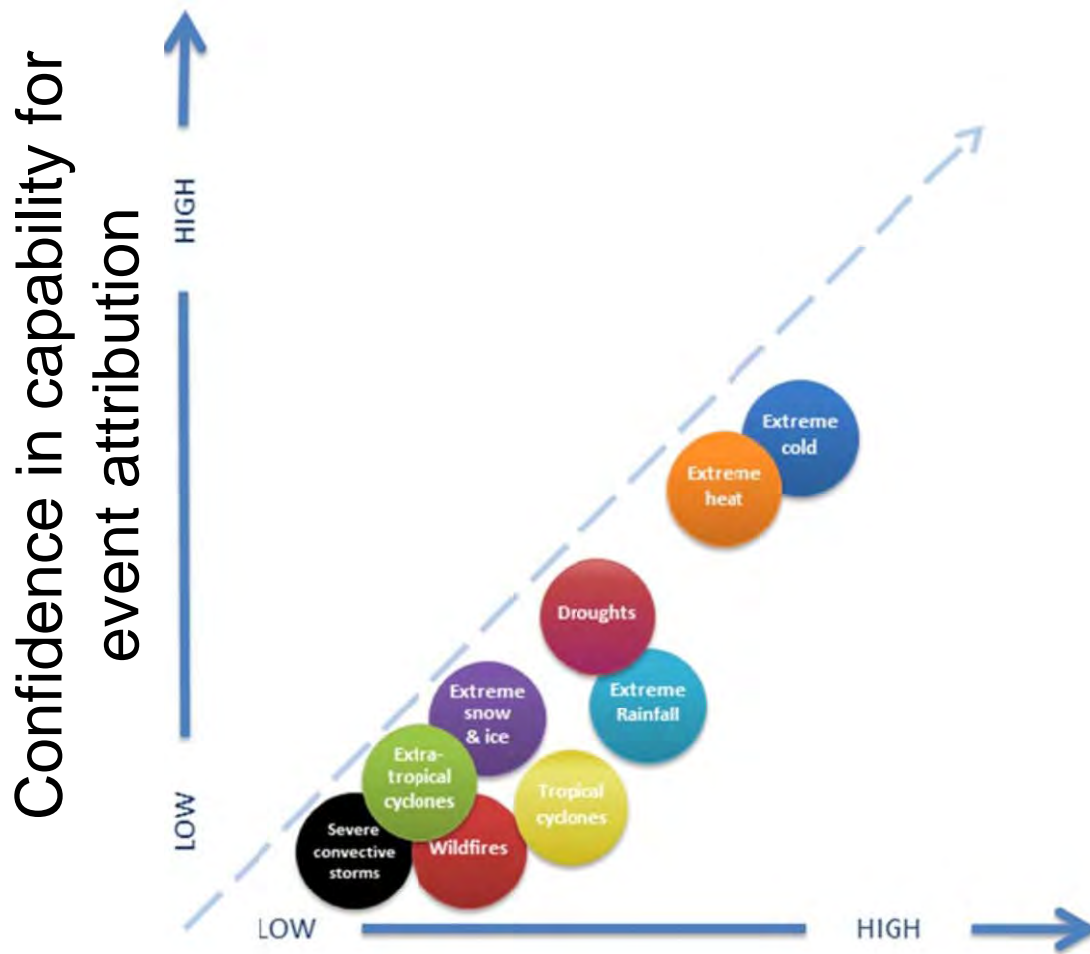
Did human influence on the climate system cause the event?



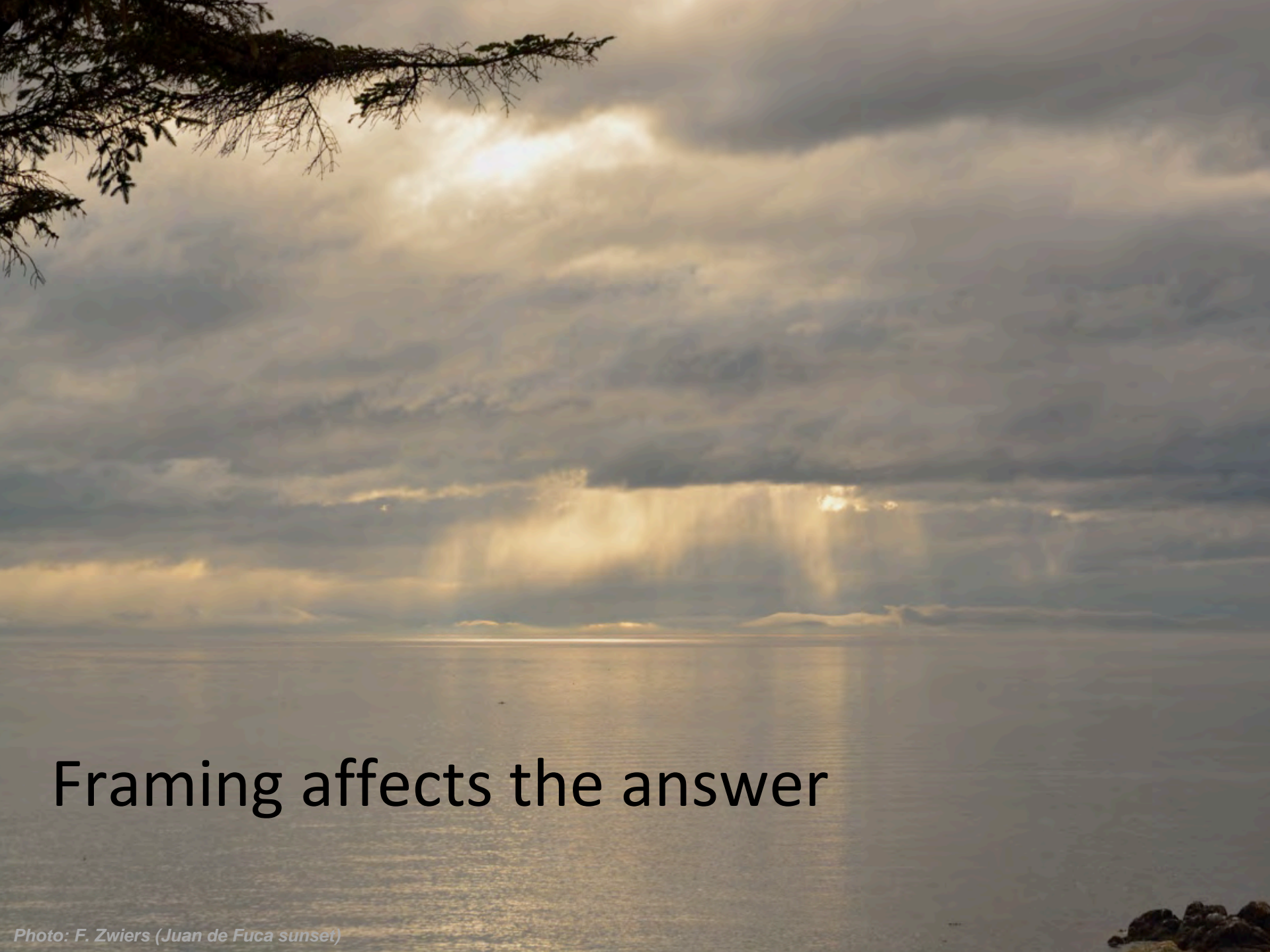
Most studies

- Most studies ask: Did it ...
 - Affect its odds? Alter its magnitude?
- Compare factual and “counterfactual” climates
 - Counterfactual → the world that might have been if we had not emitted the ~600GtC (and counting) that have been emitted since preindustrial
- These studies almost always
 - Define a class of events rather than a single event
 - Use a probabilistic approach
- Shepherd ([2016](#)) defines this as “risk based”
 - Contrasts it with a “storyline” based approach
 - i.e., analysis of the specific event that occurred

Status recently assessed by US NAS



Understanding of effect of climate change on event type



Framing affects the answer

Fort Mac Fire – May through July 2016

- 590,000 ha burnt
- 88,000 people displaced
- 2 fatalities (indirect)
- 2400 homes and 665 work camp units destroyed
- \$3.6 B CDN insured losses

Mandatory evacuation. Photo, [Jason Franson/CP](#)



Avian escape. Photo, [Mark Blinch/Reuters](#)



Edmonton Expo Centre at Northlands. Photo, [Chris Bolin](#)

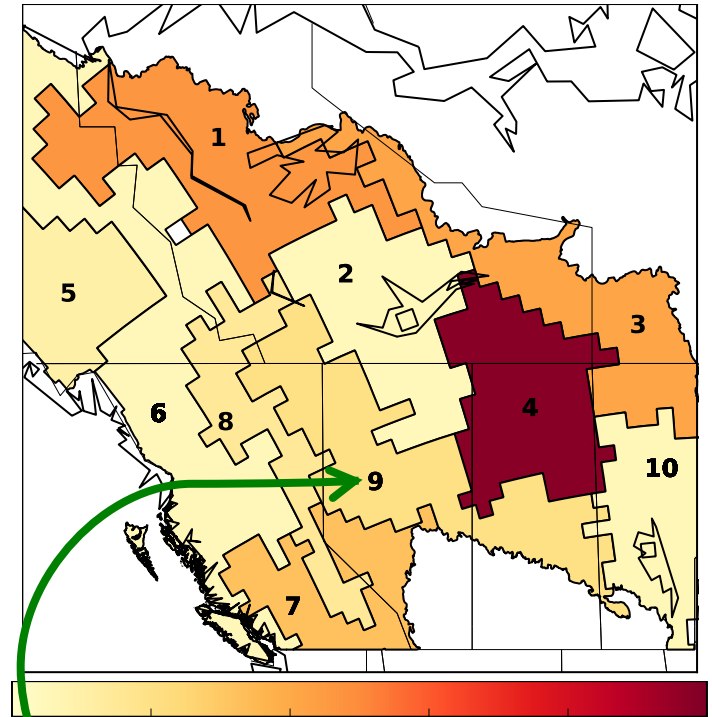


Timberlea. Photo, [Chris Bolin](#)

Fire risk (Kirchmeier-Young et al, [2017](#))

- We ask whether human induced climate change has affected fire risk in the “Southern Prairie” Homogeneous Fire Regime zone
- Measure fire risk using “CWFIS” system indicators
 - Fire Weather Index
 - Fine Fuels Moisture Code
 - Duff Moisture Code
 - Drought Code
 - Etc
- These indices depend on temperature, relative humidity, wind speed, and precipitation

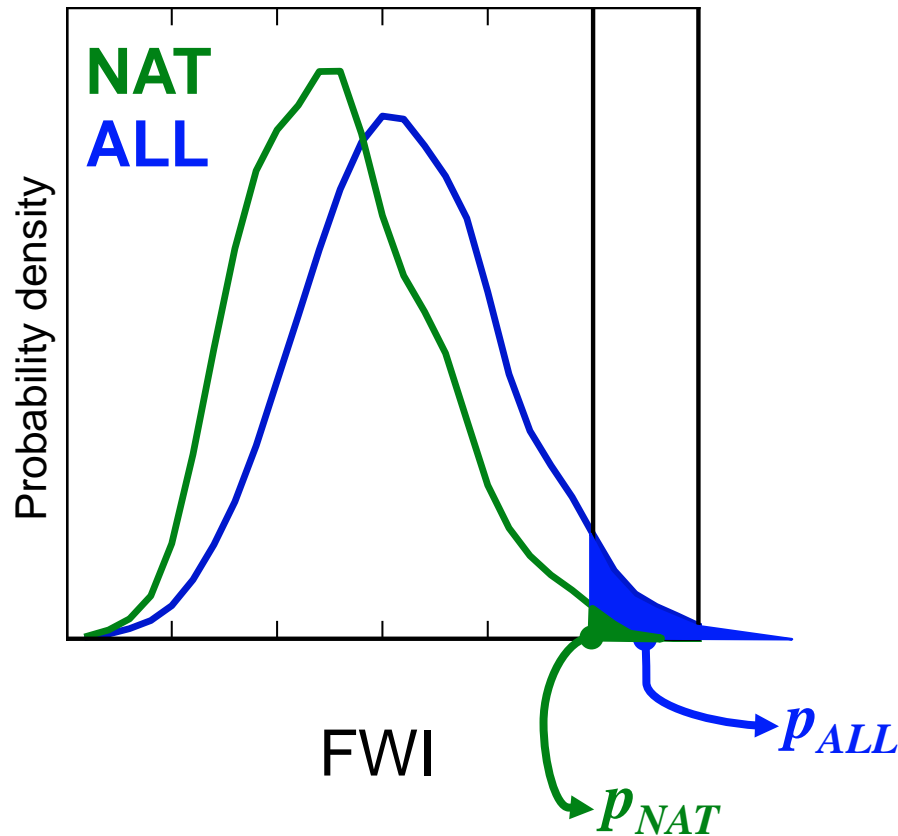
Annual area burned 1981-2010
Canadian National Fire Database



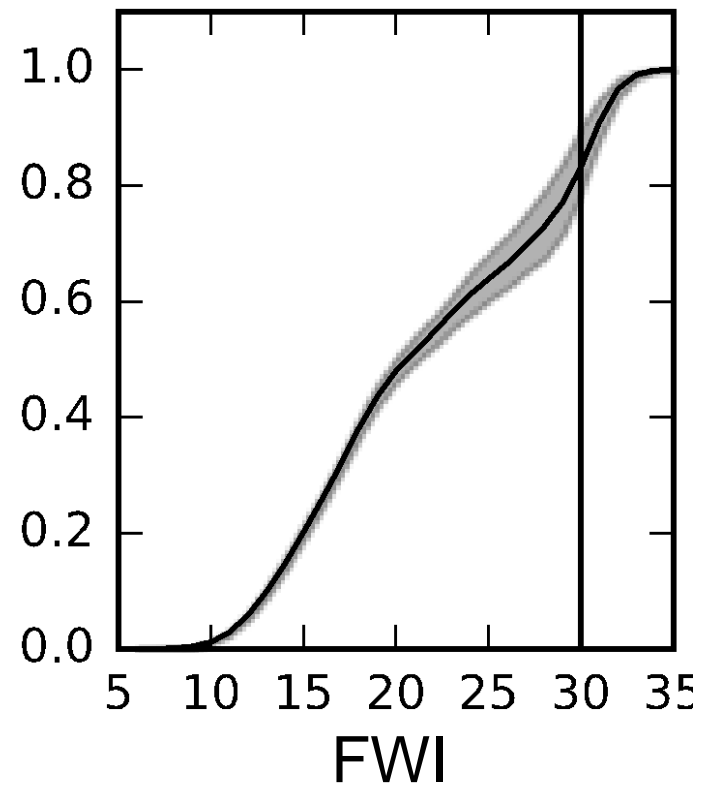
Southern Prairie HFR Zone

Fire Weather Index for Southern Prairies

HFR for the current decade (2011-2020)




$$FAR = \frac{p_{ALL} - p_{NAT}}{p_{ALL}}$$



CWFIS “Extreme” FWI level = 30

Observed FWI level in Fort Mac area \approx 40

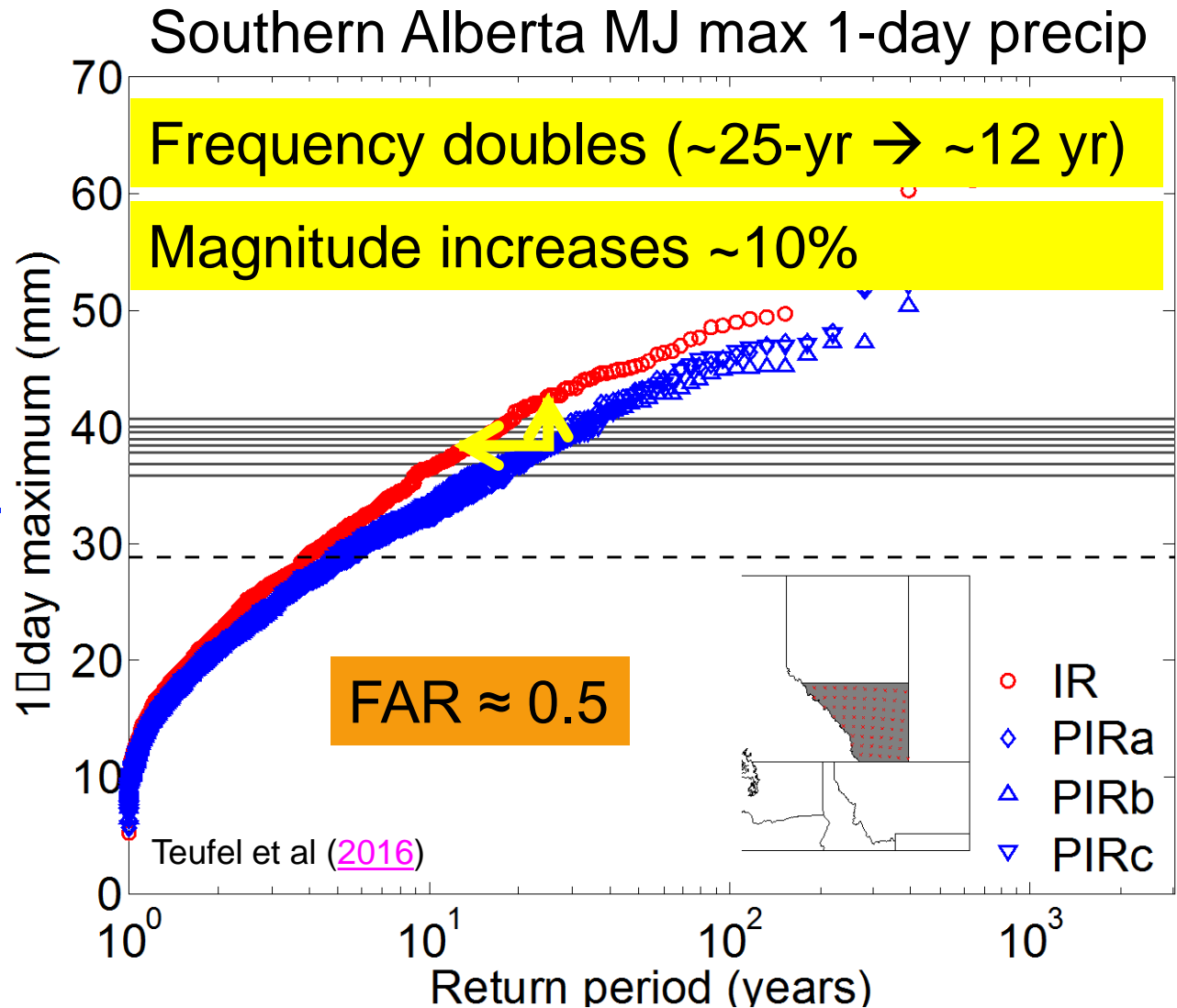
Calgary flood, 2013

- 
- 100,000 displaced, 5 deaths
 - Costliest (?) disaster event in Canadian history
 - Estimated \$5.7B USD loss (\$1.65B USD insured)

Calgary East Village (June 25, 2013), courtesy [Ryan L.C. Quan](#)

Calgary floods

Distribution of annual May-June maximum 1-day southern-Alberta precipitation in CRCM5 under **factual** and **counter-factual** conditions (conditional on the prevailing global pattern of SST anomalies)

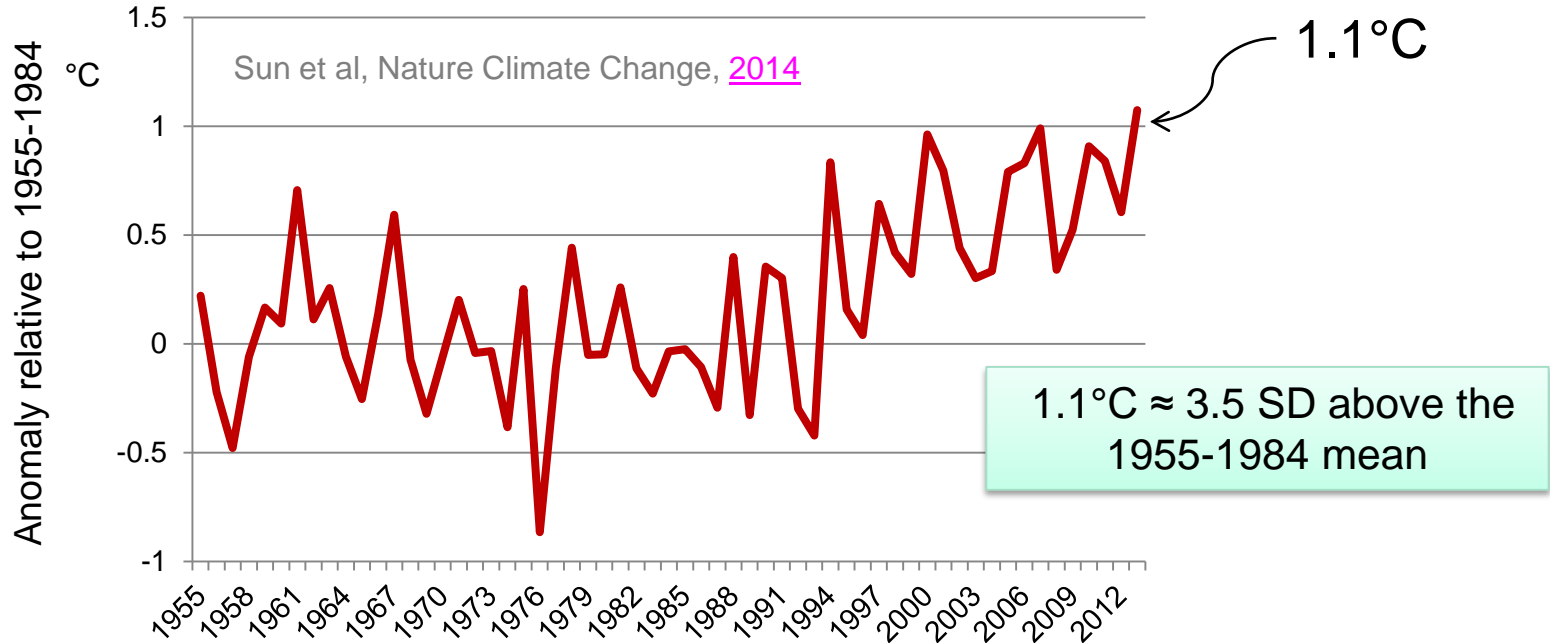


China's Hot Summer of 2013

- Impacts included estimated \$10B USD agricultural yield loss



How rare was JJA of 2013?



- Estimated event frequency
 - once in 270-years in control simulations
 - once in 29-years in “reconstructed” observations
 - once in 4.3 years relative to the climate of 2013
- Fraction of Attributable Risk in 2013: $(p_1 - p_0)/p_1 \approx 0.984$
- Prob of “sufficient causation”: $PS = 1 - ((1 - p_1)/(1 - p_0)) \approx 0.23$

Projected event frequency

— RCP4.5

— RCP8.5

+ + Frequency
x x

- - - Mean temp
- - -

23%, 4.3-yr →

Conclusions



Conclusions

- Understanding of the impact of anthropogenic forcing on observed extremes remains limited
 - Relatively high confidence for temperature extremes
 - Some confidence in precipitation extremes
 - Can say relatively little about storms, droughts, floods
- Often very limited by data (models and methods can be improved; historical data is much harder)
- Need further methodological development and improved process understanding
- Event attribution is increasingly undertaken
 - Still much work to do to develop methods and capabilities, understand implications of framing choices, and develop objective evaluation techniques



Questions?

<https://www.pacificclimate.org/>

Photo: F. Zwiens